# **Unit 2 Microoperations**

Combinational and sequential circuits can be used to create simple digital systems. These are the low-level building blocks of a digital computer. The operations on the data in registers are called microoperations. Examples of micro-operations are

- Shift
- Load
- Clear
- **Increment**

Alternatively we can say that an elementary operation performed during one clock pulse on the information stored in one or more registers is called micro-operation. The result of the operation may replace the previous binary information of the resister or may be transferred to another resister. Register transfer language can be used to describe the (sequence of) micro-operations.

## **Microoperation types**

The microoperations most often encountered in digital computers are classified into 4 categories:

- 1. Register transfer microoperations
- 2. Arithmetic microoperations
- 3. Logic microoperations
- 4. Shift microoperations

## **1. Resister transfer microoperations**

Registers are designated by capital letters, sometimes followed by numbers (e.g., A, R13, IR). Often the names indicate function:



Information transfer from one register to another is described in symbolic form by replacement operator. The statement "R2  $\leftarrow$ R1" denotes a transfer of the content of the R1 into resister R2.

## **Control Function**

Often actions need to only occur if a certain condition is true. In digital systems, this is often done via a control signal, called a control function.

Example: P:  $R2 \leftarrow R1$  i.e. if (P = 1) then (R2  $\leftarrow R1$ ) Which means "if P = 1, then load the contents of register R1 into register R2". If two or more operations are to occur simultaneously, they are separated with commas.

Example: P: R3  $\leftarrow$  R5, MAR  $\leftarrow$  IR

## **2. Arithmetic microoperations**

- The basic arithmetic microoperations are
	- Addition
	- Subtraction
	- **Increment**
	- Decrement
- The additional arithmetic microoperations are
	- Add with carry
	- Subtract with borrow
	- Transfer/Load





## **Binary Adder**

To implement the add microoperation with hardware, we need the resisters that hold the data and the digital component that performs the arithmetic addition. The digital circuit that generates the arithmetic sum of two binary numbers of any lengths is called **Binary adder**. The binary adder is constructed with the full-adder circuit connected in cascade, with the output carry from one full-adder connected to the input carry of the next fulladder.



Fig.: 4-bit binary adder

An n-bit binary adder requires n full-adders. The output carry from each full-adder is connected to the input carry of the next-high-order-full-adder. Inputs A and B come from two registers R1 and R2.

## **Binary Subtractor**

The subtraction A – B can be done by taking the 2's complement of B and adding to A. It means if we use the inverters to make 1's complement of B (connecting each B to an inverter) and then add 1 to the least significant bit (by setting carry  $C_0$  to 1) of binary adder, then we can make a binary subtractor.



## **Binary Adder-Subtractor**

**Question**: *How binary adder and subtractor can be accommodated into a single circuit? explain.* The addition and subtraction operations can be combined into one common circuit by including an exclusive-OR gate with each full-adder.



Fig.: 4-bit adder-subtractor

The mode input M controls the operation the operation. When M=0, the circuit is an adder and when M=1 the circuit becomes a subtractor. Each exclusive-OR gate receives input M and one of the inputs of B.

- When M=0:  $B<sup>®</sup> M = B<sup>®</sup> O = B$ , i.e. full-adders receive the values of B, input carry is B and circuit performs A+B.
- When M=1:  $B \oplus M = B \oplus 1 = B'$  and  $C_0 = 1$ , i.e. B inputs are all complemented and 1 is added through the input carry. The circuit performs  $A + (2's$  complement of B).

### **Binary Incrementer**

The increment microoperation adds one to a number in a register. For example, if a 4-bit register has a binary value 0110, it will go to 0111 after it is incremented. Increment microoperation can be done with a combinational circuit (half-adders connected in cascade) independent of a particular register.



Fig.: 4-bit binary Incrementer

## **Arithmetic Circuit**

The arithmetic microoperations can be implemented in one composite arithmetic circuit. By controlling the data inputs to the adder (basic component of an arithmetic circuit), it is possible to obtain different types of arithmetic operations.

In the circuit below contains:

- 4 full-adders
- 4 multiplexers (controlled by selection inputs S0 and S1)
- two 4-bit inputs A and B and a 4-bit output D
- Input carry  $c_{in}$  goes to the carry input of the full-adder.

Output of the binary adder is calculated from the arithmetic sum:  $D = A + Y + c_{in}$ .

By controlling the value of Y with the two selection inputs S1 & S0 and making  $\theta$  or 1, it is possible to generate the 8 arithmetic microoperations listed in the table below:



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Fig: 4-bit arithmetic circuit

## **3. Logic microoperations**

**Question**: *What do you mean by Logic microoperations*? *Explain with its applications.* **Question**: *How Logic microoperations can be implemented with hardware*?

Logic microoperations are bit-wise operations, i.e., they work on the individual bits of data. Useful for bit manipulations on binary data and for making logical decisions based on the bit value. There are, in principle, 16 different logic functions that can be defined over two binary input variables. However, most systems only implement four of these

– AND (^), OR (۷), XOR (⊕), Complement/NOT

The others can be created from combination of these four functions.

#### **Hardware implementation**

Hardware implementation of logic microoperations requires that logic gates be inserted be each bit or pair of bits in the resisters to perform the required logic operation.



(a) Logic diagram

## **Applications of Logic Microoperations**

Logic microoperations can be used to manipulate individual bits or a portion of a word in a register. Consider the data in a register A. Bits of register B will be used to modify the contents of A.



#### **Selective-set**

In a selective set operation, the bit pattern in B is used to *set* certain bits in A.



1 1 1 0  $A_{t+1}$   $(A \leftarrow A + B)$ 

 $(A \leftarrow A \oplus B)$ 

Bits in resister A are set to 1 when there are corresponding 1's in resister B. It does not affect the bit positions that have 0's in B.

#### **Selective-complement**

In a selective complement operation, the bit pattern in B is used to *complement* certain bits in A.



If a bit in B is 1, corresponding position in A get complemented from its original value, otherwise it is unchanged.

#### **Selective-clear**

In a selective clear operation, the bit pattern in B is used to *clear* certain bits in A.



If a bit in B is 1, corresponding position in A is set to 0, otherwise it is unchanged.

#### **Mask Operation**

In a mask operation, the bit pattern in B is used to *clear* certain bits in A.



#### **Clear Operation**

In clear operation, if the bits in the same position in A and B same, that bit in A is cleared (putting 0 there), otherwise same bit in A is set(putting 1 there). This operation is achieved by exclusive-OR microoperation.



#### **Insert Operation**

An insert operation is used to introduce a specific bit pattern into A register, leaving the other bit positions unchanged.

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This is done as

- A **mask (ANDing)** operation to clear the desired bit positions, followed by
- An **OR** operation to introduce the new bits into the desired positions
- Example
	- » Suppose you want to introduce 1010 into the low order four bits of A:



## **4. Shift microoperations**

**Question**: *What do you mean by shift microoperations*? Explain its types.

**Question**: *Is there a possibility of Overflow during arithmetic shift? If yes, how it can be detected?* Shift microoperations are used for serial transfer of data. They are also used in conjunction with arithmetic, logic and other data processing operations. The contents of a resister can be shifted left or right. There are three types of shifts

- 1. Logical shift
- 2. Circular shift
- 3. Arithmetic shift



## **1. Logical shift**

A logical shift is one that transfers 0 through the serial input. In a Register Transfer Language, the following notation is used



Examples:

 $R2 \leftarrow$  *shr* R2

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#### **2. Circular Shift** (rotate operation)

Circular-shift circulates the bits of the resister around the two ends without the loss of information.

#### **Right circular shift operation**



#### **Left circular shift operation:**



In a RTL, the following notation is used

- *cil* for a circular shift left
- *cir* for a circular shift right
- Examples:
- $R2 \leftarrow$  *cir* R2  $R3 \leftarrow$  *cil* R3

## **3. Arithmetic shift**

An arithmetic shift is meant for signed binary numbers (integer). An arithmetic left shift multiplies a signed number by 2 and an arithmetic right shift divides a signed number by 2. Arithmetic shifts must leave the sign bit unchanged because the sign of the number remains the same when it is multiplied or divided by 2. The left most bit in a resister holds a sign bit and remaining hold the number. Negative numbers are in 2's complement form.

In a Resister Transfer Language, the following notation is used

- *ashl* for an arithmetic shift left
- *ashr* for an arithmetic shift right
- Examples:

 $\gg$  R<sub>2</sub>  $\leftarrow$  *ashr* R<sub>2</sub>

 $\gg$  R<sub>3</sub>  $\leftarrow$  ashl<sub>R3</sub>

### **Arithmetic shift-right**

Arithmetic shift-right leaves the sign bit unchanged and shifts the number (including a sign bit) to the right. Thus  $R_{n-1}$  remains same;  $R_{n-2}$  receives input from  $R_{n-1}$  and so on.



#### **Arithmetic shift-left**

Arithmetic shift-left inserts a 0 into R<sub>0</sub> and shifts all other bits to left. Initial bit of R<sub>n-1</sub> is lost and replaced by the bit from  $R_{n-2}$ .

#### **Overflow case during arithmetic shift-left:**

If a bit in  $R_{n-1}$  changes in value after the shift, sign reversal occurs in the result. This happens if the multiplication by 2 causes an overflow.

Thus, left arithmetic shift operation must be checked for the overflow: an overflow occurs after an arithmetic shift-left if before shift  $R_{n-1} \neq R_{n-2}$ .



#### **Hardware implementation of shift microoperations**

A combinational circuit shifter can be constructed with multiplexers as shown below:



Fig: 4-bit combinational circuit shifter

## **Arithmetic Logic Shift Unit**

This is a common operational unit called arithmetic logic unit (ALU). To perform a microoperation, the contents of specified registers are placed in the inputs of the common ALU. The ALU performs the operation and transfer result to destination resister.



Fig: One stage of arithmetic logic shift unit



Table: Function table for Arithmetic logic shift unit

EXERCISES: Textbook chapter 4→ 4.8, 4.13, 4.17, 4.18, 4.19, 4.21

4.8(Solution)





4.17(Solution)

